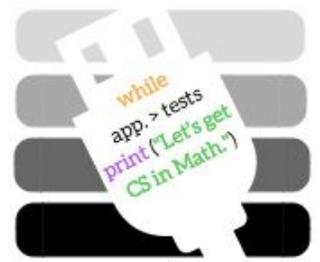


Playful Polygons - #CSandMath



@dandersod

Lesson Credit:

This lesson was first presented by Dan Anderson (@dandersod) at the 2016 NCTM Annual in his session titled [Geometry from Scratch](#)

Project Goal:

Students will use their knowledge of interior and exterior polygon angles to draw various regular shapes. They will then extend that understanding to the generalizations of equations for those angles, and explore some artistic applications.

Standards:

6.3.2.3 Develop and use formulas for the sums of the interior angles of polygons by decomposing them into triangles.

9.3.3.7 Use properties of polygons-including quadrilaterals and regular polygons-to define them, classify them, solve problems and logically justify results.

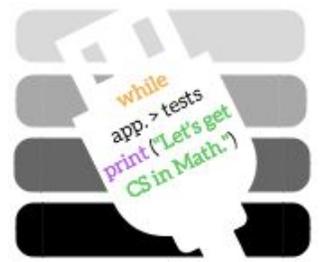
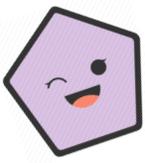
Student Handout [Linked Here](#)

Teacher Guide:

Challenge 1: Resist the urge to just model how to make a square as an opening example. Give them basics like how to link blocks, pixel distance understanding, etc...but don't cheat them out of the original aha moment! Instead encourage collaboration with peers and celebrate their struggles and eventual successes :) After students have had a chance to play with the square and triangle, pull them back together and go over the code variations on the next page and have a conversation about efficiency and draw up the regular triangle on the board to talk about turning the exterior angle.

For the rest of the challenges, it's probably in your best interest to try all of them first hand before your students. Give yourself permission to feel good about your own struggles without first looking at the solutions.





Possible square solutions:

Here are two common snips of code used by students to make their squares. Did you notice the pattern of moving the same length and turning 90 degrees? Do you see how the repeat loops can help to make the code more efficient? What about turning the exterior angle instead of the interior angle? Most students reported this as their biggest hang up for challenge 1!

```
when green flag clicked
  pen down
  repeat 3
    move 100 steps
    turn 120 degrees
```

Exterior Angle :)

```
when green flag clicked
  clear
  pen down
  move 100 steps
  turn 90 degrees
  pen up
```

```
when green flag clicked
  clear
  pen down
  repeat 4
    move 100 steps
    turn 90 degrees
  pen up
```

Possible Solutions to Challenge 1: Polygons

Triangle

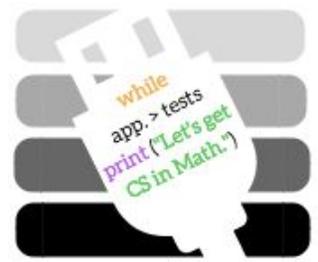
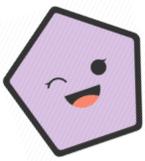
```
when green flag clicked
  clear
  pen down
  repeat 3
    move 100 steps
    turn 120 degrees
```

Pentagon

```
when green flag clicked
  clear
  pen down
  repeat 5
    move 100 steps
    turn 72 degrees
```

Hexagon

```
when green flag clicked
  clear
  pen down
  repeat 6
    move 100 steps
    turn 60 degrees
```



Challenge 2: N-Gon Maker

Note that students could have taken $180 - ((n-2)*180)$ for the turn formula. Although not quite as efficient, this is strong student thinking that should receive validation :)

```

when clicked
  ask "How many sides?" and wait
  set n to answer
  repeat n
    move 75 steps
    turn 360 / n degrees
  
```

Challenge 3: Cascading Convex

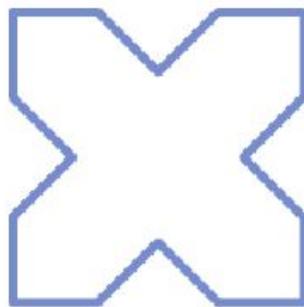
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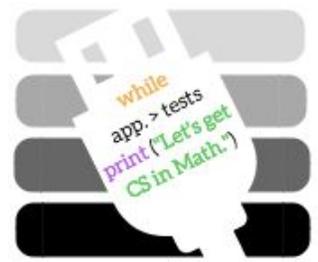
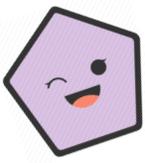
when clicked
  Initialize
  ask "How many sides to start?" and wait
  set n to answer
  pen down
  repeat until n = 12
    repeat n
      move 75 steps
      turn 360 / n degrees
    change n by 1
    set pen color to pick random 500 to 1000
  
```

Challenge 3: Example artistic release classic concaved polygon

```

when clicked
  ask "length?" and wait
  set n to answer
  pen down
  set pen color to purple
  set pen size to 4
  move n steps
  repeat 4
    turn 45 degrees
    move n steps
    turn 90 degrees
    move n steps
    turn 45 degrees
    move n steps
    turn 90 degrees
    move n steps
  
```





Challenge 4: Polygon Illusion (Possible Solution)

```
when clicked
  clear
  pen up
  point in direction 90
  glide 1 secs to x: 0 y: -5
  ask "How many sides? (3-8 for best look)" and wait
  set n to answer
  ask "side length? (Start small...like 0-20)" and wait
  set d to answer
  set a to 360 / n
  set pen color to 
  set pen size to 2
  repeat until y position > 170
    pen down
    move d steps
    turn a degrees
    set d to d + 1
    turn 2 degrees
    change pen color by 4
```